

FPGA SYSTEM ERROR RATE ANALYSIS FOR HARSH RADIATION ENVIRONMENTS



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Outline

2

- Introduction
- Background
 - FPGA Radiation Effects
 - Mitigating FPGA Radiation Effects
 - Harsh Radiation Environments
- Test Methodology
 - Fault Injection
 - Proton Accelerator
- Results
 - Fault Injection
 - Proton Accelerator
- SEU Rate Models
- Estimating Probability of Failure
- Conclusion



Introduction

3

- FPGA computation capabilities
 - ▣ FPGAs are well-suited to remote-sensing, comms and other DSP applications often used in space
- Large percentage of FPGA space applications target LEO
 - ▣ LANL CFE, NASA GRACE, U. Southern Australia FedSat, NASA TACSAT-2, etc.
- We want to extend the reach of FPGAs to more interesting orbits
 - ▣ e.g. GPS, GEO, Molniya, Polar, etc.



Background :: FPGA Radiation Effects

4

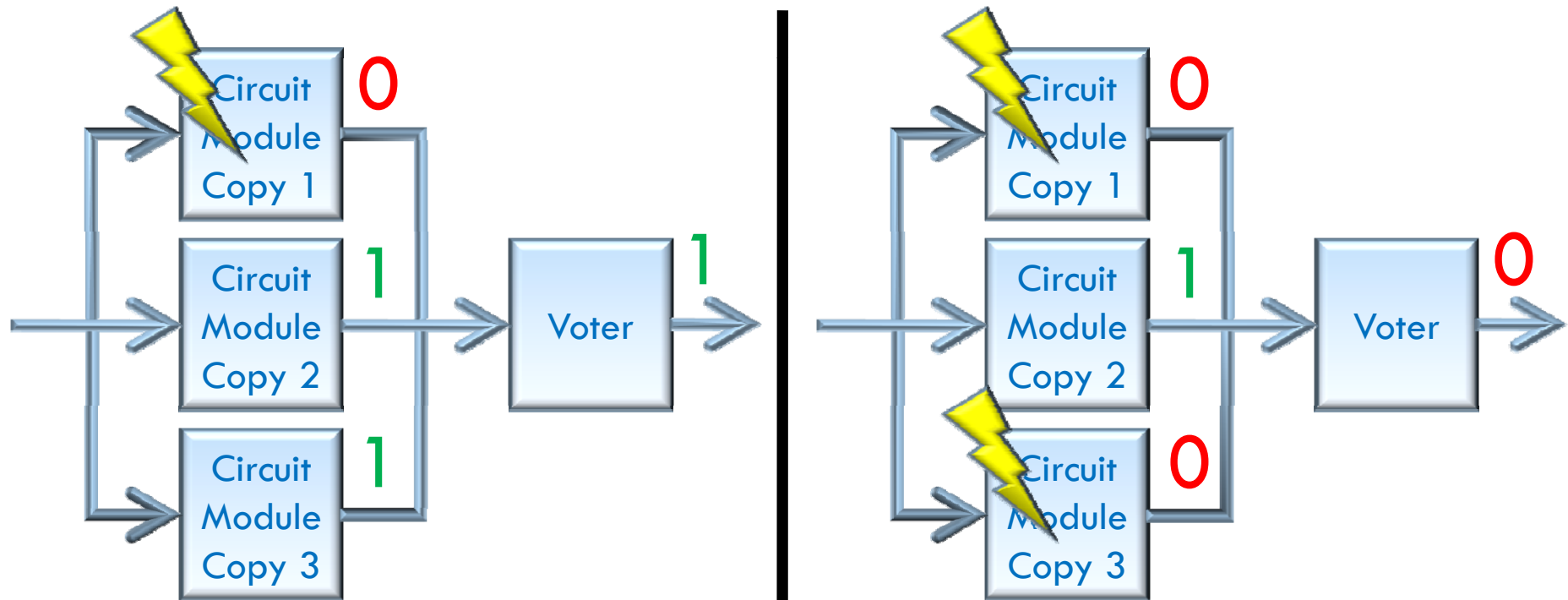
- Single Event Upsets (SEU)
 - ▣ Change of state in memory structure
 - ▣ A significant portion of SRAM-based FPGA memory cells are dedicated to the user's circuit design (configuration memory)
 - ▣ SEUs in the configuration memory can modify the actual operation of the circuit
- Mitigating FPGA Radiation Effects
 - ▣ Triple modular redundancy (TMR)
 - XTMR style of TMR with triplicated voters must be employed to eliminate all single points of failure
 - ▣ Scrubbing
 - Periodic or continuous refresh of configuration memory back to intended state
 - Prevents accumulation of upsets in configuration memory
 - Reduces probability of simultaneous upsets (i.e. multiple independent upsets, MIUs) in configuration memory



Background :: Mitigating FPGA Radiation Effects (cont.)

5

- Multiple independent upsets (MIUs) can defeat TMR and scrubbing



SEU is *masked* by TMR

MIUs defeat TMR



Background :: Harsh Radiation Environments

6

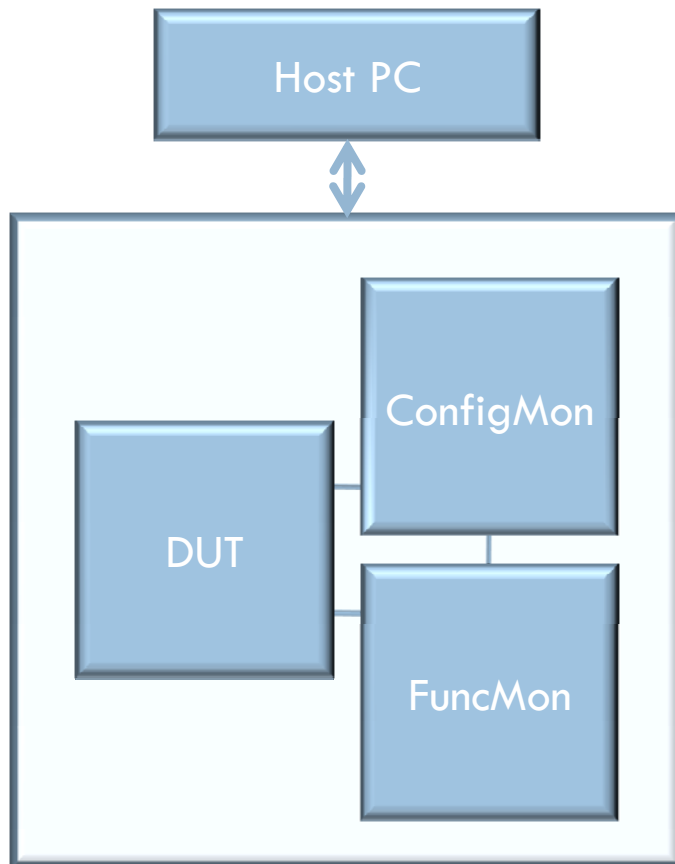
- Solar energetic particle (SEP) events (colloquially known as solar flares)
 - Harshlest radiation environment in space Earth orbits (Tylka et al.)
 - SEU rate can increase orders of magnitude
 - Modeled in CREME96 by week-long event in October 1989
 - Primarily affect orbits further away from the Earth's magnetic field or at the poles (e.g. GPS, GEO, Molniya, Polar)
- An increase in SEU rate increases the likelihood of MIUs
- *The purpose of this work was to measure the probability of failure from MIUs during SEP events*



Testing Methodology :: Fault Injection

7

- DUT = Xilinx Virtex-4 XC4VSX55



Test Fixture

- Algorithm

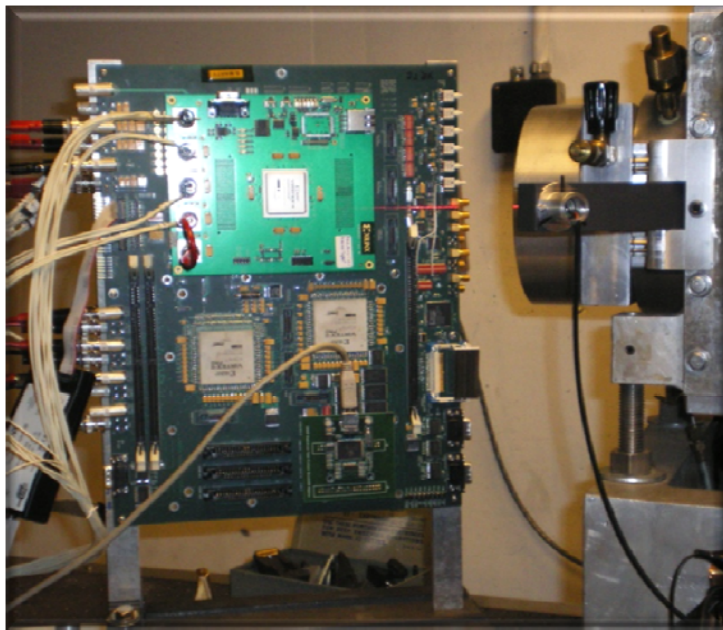
```
do {
    ○ generate 'i' random bits
      to upset
    ○ inject 'i' upsets into
      bitstream
    ○ check for output error
    ○ fix upset bits
    ○ reset device
    ○ record data to output
      file
} while trials < 'm'
```



Testing Methodology :: Accelerator

8

- DUT = Xilinx Virtex-4 XC4VSX55
- Crocker Nuclear Laboratory, UC Davis
- 63 MeV Protons



- Algorithm

```
do {  
  ○ sleep for time 't'  
  ○ get and fix upset frames  
  ○ if upsets found  
    ○ record upsets to file  
    ○ check for output error  
  ○ reset DUT  
} while time < 'T'
```

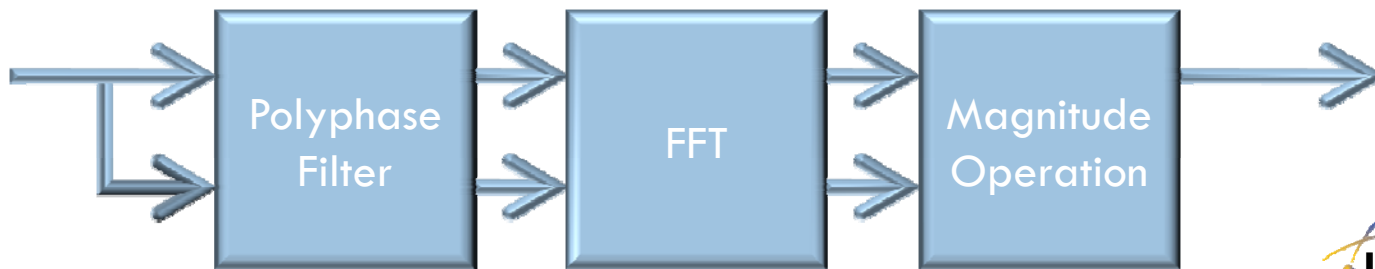


Results :: Example Circuits

9

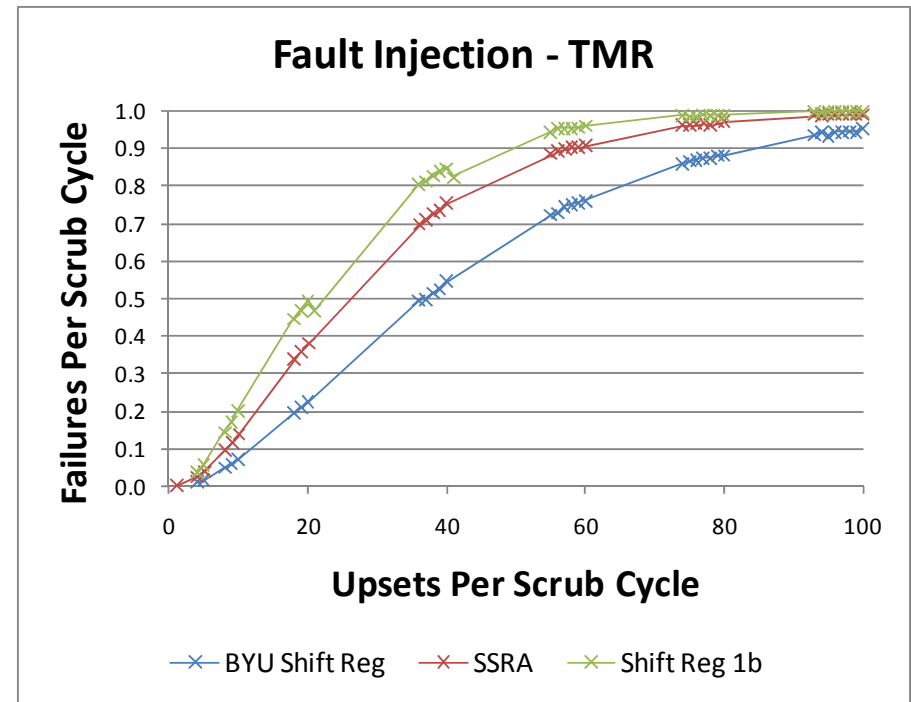
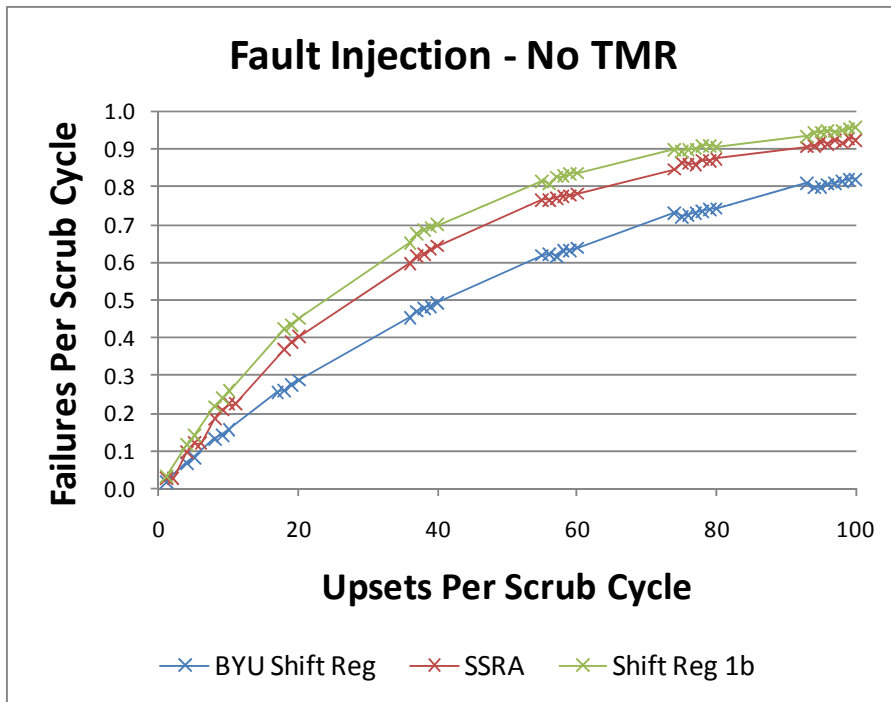
- **BYU Shift Reg**
 - 32-bit wide, 250 stage shift register with arbitrary combinational logic between each stage
- **Shift Reg 1 b**
 - 1-bit wide, 16,200 stage shift register
- **SSRA**
 - Digital signal processing kernel

Design	Design Utilization - Slices	
	No TMR	TMR
BYU Shift Reg	4011 (16%)	12014 (48%)
Shift Reg 1 b	8111 (33%)	24314 (98%)
SSRA	5381 (21%)	18591 (75%)



Results :: Fault Injection

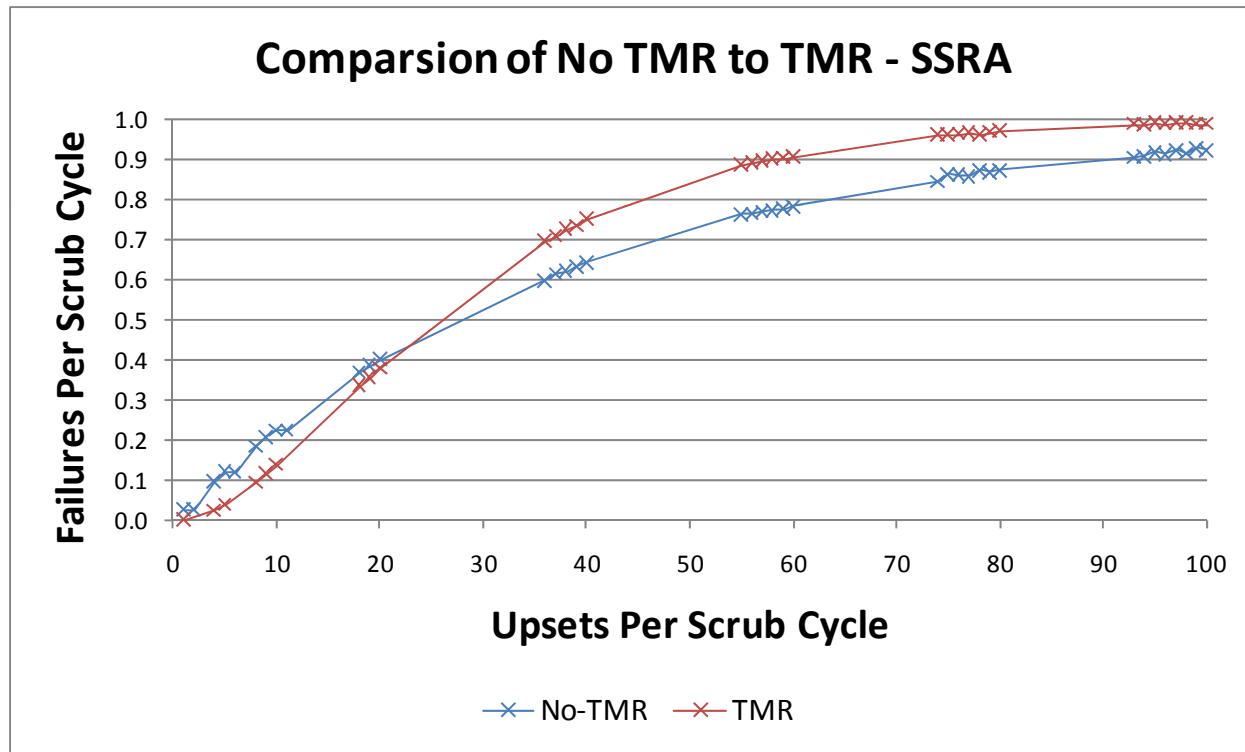
10



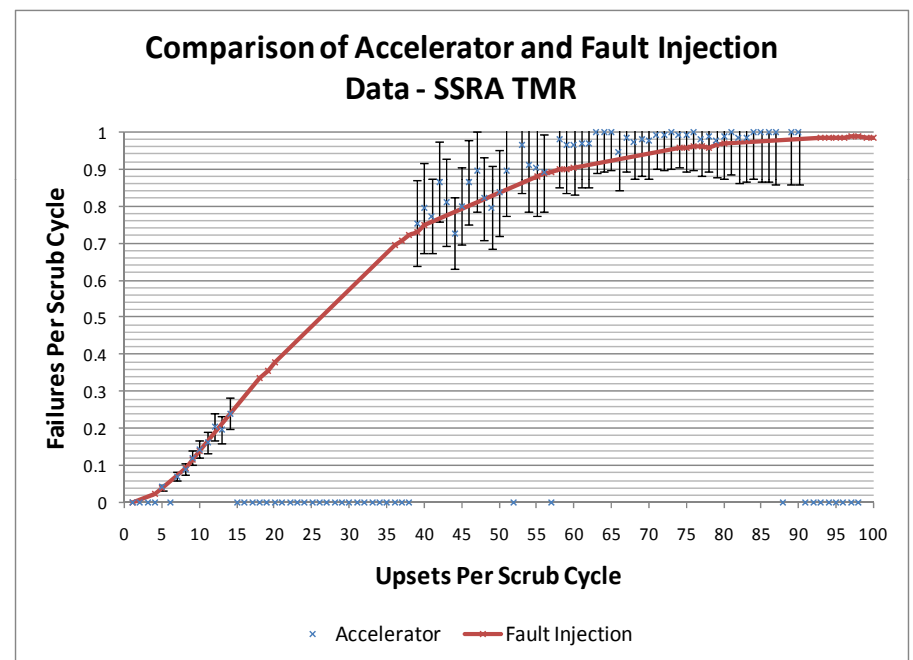
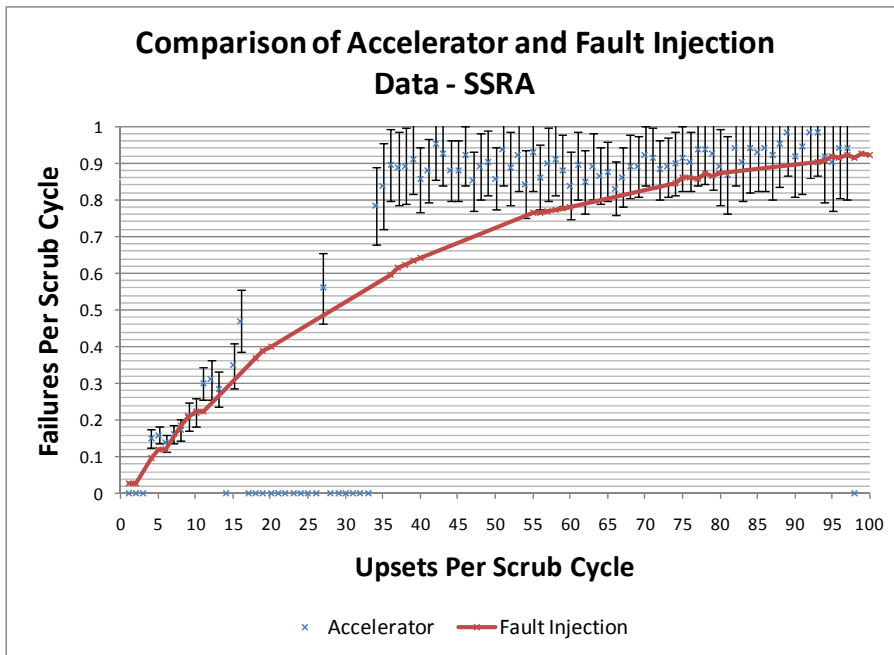
Note: A minimum of 1000 events were observed for each data point.



Results :: Fault Injection



Results :: Accelerator



Note: A minimum of 30 events were observed for each data point.



SEU Rate Models

13

Orbit	Apogee (km)	Perigee (km)	Inclination (deg)	Peak 5-Minute SEU Rate (SEUs/Device/s)
GEO	35786	35786	0	3.29E-1
GPS	20200	20200	55	2.85E-1
Molniya	39305	1507	63.2	3.08E-1
Polar	833	833	98.7	7.84E-2

□ SEU Rate Models

- CREME96: Worst Week, Worst Day, Peak 5-minutes (see data above)
- What actually happens during that peak 5-minutes?
 - Real Answer: Nobody Knows!!
 - But we can bound the problem...
 - Best Case: Fluence is perfectly averaged over 5 minutes
 - Worst Case: Fluence all comes during one scrub cycle



Estimating Probability of Failure

14

- Goal: Estimate probability of failure $P(F_{5\text{-min}})$ for the CREME96 peak 5 minutes
 - Requires probability of i upsets per scrub cycle $P(A_i)$
 - Requires conditional probability of failure for a particular scrub cycle given i upsets occurred during that particular scrub cycle $P(F_{1\text{-cycle}} | A_i)$
 - Requires probability of failure $P(F_{1\text{-cycle}})$ for one trial (i.e. one scrub cycle)
- We measured $P(F_{1\text{-cycle}} | A_i)$ using fault injection and the accelerator
- We assume that $P(A_i)$ has a Poisson probability density function (pdf) since $n \gg 1$ and $t_a \ll T$; with parameter $\lambda = (t_a * n)/T$, i.e. $\lambda =$ the SEU rate
 - $T =$ interval, e.g. 5 minutes
 - $n =$ number of upsets, e.g. 100 upsets in peak 5 minutes
 - $t_a =$ length of sub-interval, e.g. 15 millisecond scrub cycle
- We calculate $P(F_{1\text{-cycle}})$ for one scrub cycle using the following equation

$$P(F_{1\text{-cycle}}) = \sum_{i=0}^{\infty} P(F_{1\text{-cycle}} | A_i) P(A_i)$$



Estimating Probability of Failure

15

- If we assume that each scrub cycle is an independent trial (valid if scrubbing works correctly), then we can use the following fundamental theorem from Bernoulli to compute $P(F_{5\text{-min}})$ over the entire 5 minute interval

$$P(F_{5\text{-min}}) = \sum_{i=1}^m \binom{m}{i} P(F_{1\text{-cycle}})^i (1 - P(F_{1\text{-cycle}}))^{m-i}$$

or

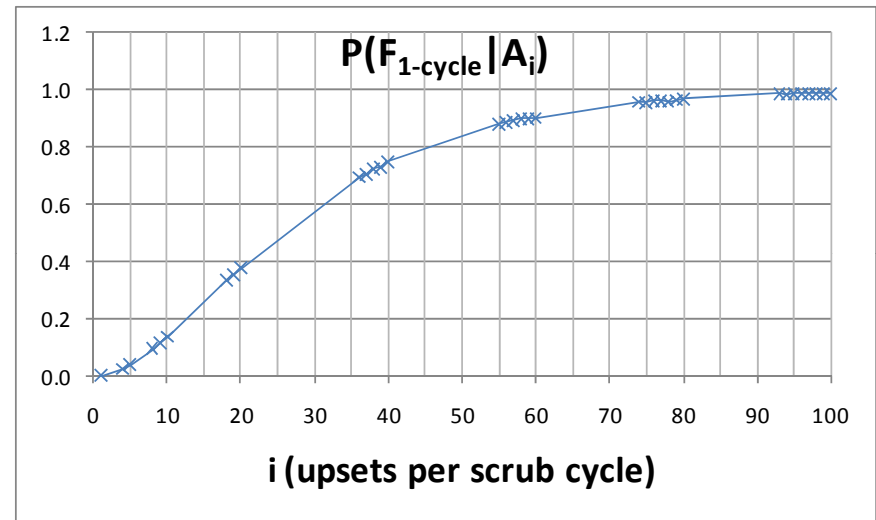
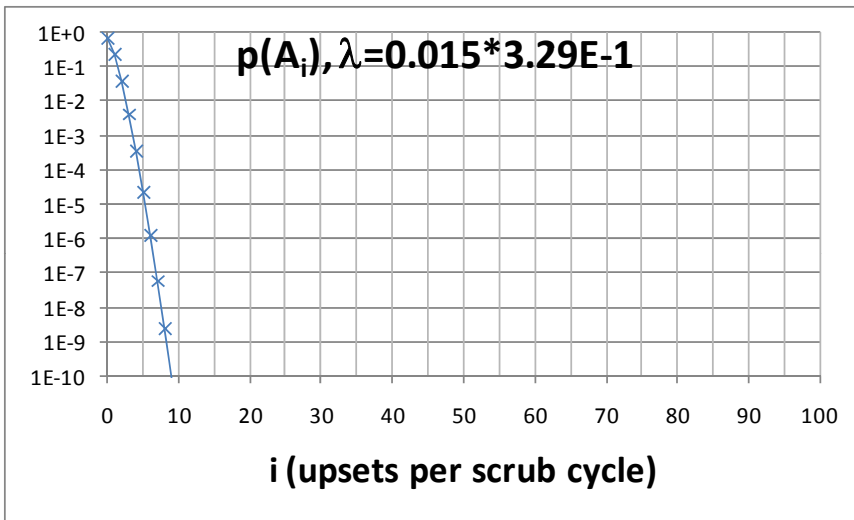
$$\begin{aligned} P(F_{5\text{-min}}) &= 1 - \sum_{i=0}^0 \binom{m}{i} P(F_{1\text{-cycle}})^0 (1 - P(F_{1\text{-cycle}}))^{m-0} \\ &= 1 - (1 - P(F_{1\text{-cycle}}))^m \end{aligned}$$

- m = number of trials (assuming 15 millisecond scrub cycle, $m=20,000$ in five minutes)



Estimating Probability of Failure :: Example (SSRA TMR design, GEO orbit, CREME96 “Best Case” model)

16



$$P(F_{1-cycle}) = \sum_{i=0}^{\infty} P(F_{1-cycle} | A_i) P(A_i)$$

$$= 9.7 \times 10^{-8}$$

$$P(F_{5-min}) = 1 - (1 - P(F_{1-cycle}))^m$$

$$= 1 - (1 - 9.7 \times 10^{-8})^{20000}$$

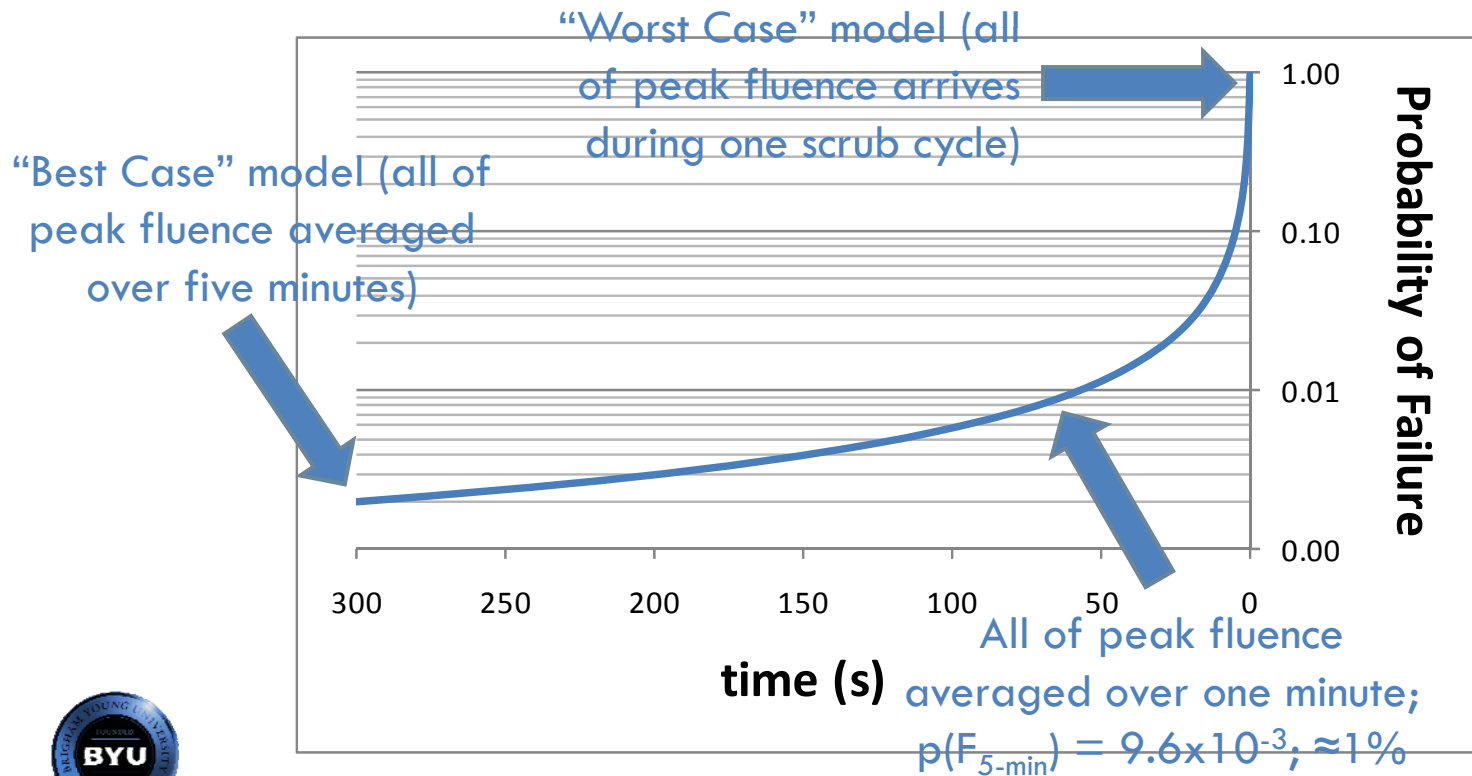
$$= 1.9 \times 10^{-3}$$



Estimating Probability of Failure :: P(F) Estimates

17

Design	Orbit	P(F _{5-min})		P(F _{worst-day})	P(F _{worst-week})
		Best Case	Worst Case		
SSRA	GEO	1.99x10 ⁻³	.987	3.3x10 ⁻²	1.8x10 ⁻²



Conclusion

18

- ❑ Multiple independent upsets (MIUs) can defeat TMR and scrubbing
- ❑ SEP events can cause MIUs, particularly in strategic orbits with little or no protection provided by the Earth's magnetic field
- ❑ An example circuit's response to various sizes of MIUs was measured using fault injection and verified at a proton accelerator
- ❑ Probability of failure can be estimated using CREME96 SEU rates and MIU response data (fault injection or accelerator), however CREME96 SEU rate data are insufficient to make high fidelity estimates
 - ❑ We tried creating a model based on an extrapolation from the CREME96 worst week, worst day and peak 5 minutes, but $p(F_{5\text{-min}})$ was approximately the same as the "best case" model
 - ❑ Better models are needed
- ❑ Probability of failure estimates for an example circuit were presented
 - ❑ $P(F) = 1.99\text{E-}3$ in the best case
 - ❑ $P(F) = .987$ in the worst case



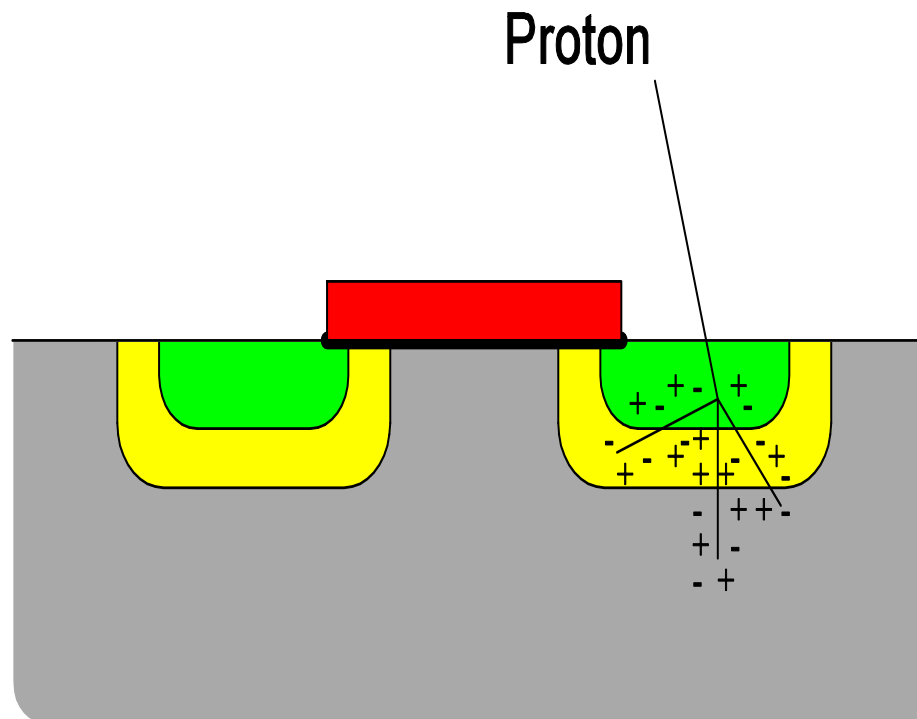
BACKUP SLIDES



Background :: Single Event Effects

20

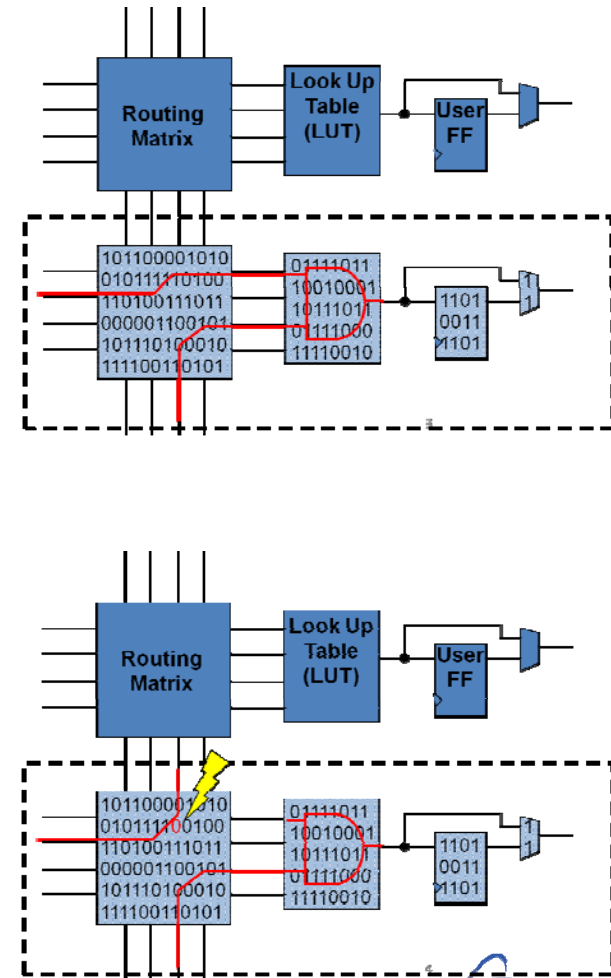
- Single Event Upsets (SEU)
 - ▣ Change of state in memory structure



Background :: FPGA Radiation Effects

21

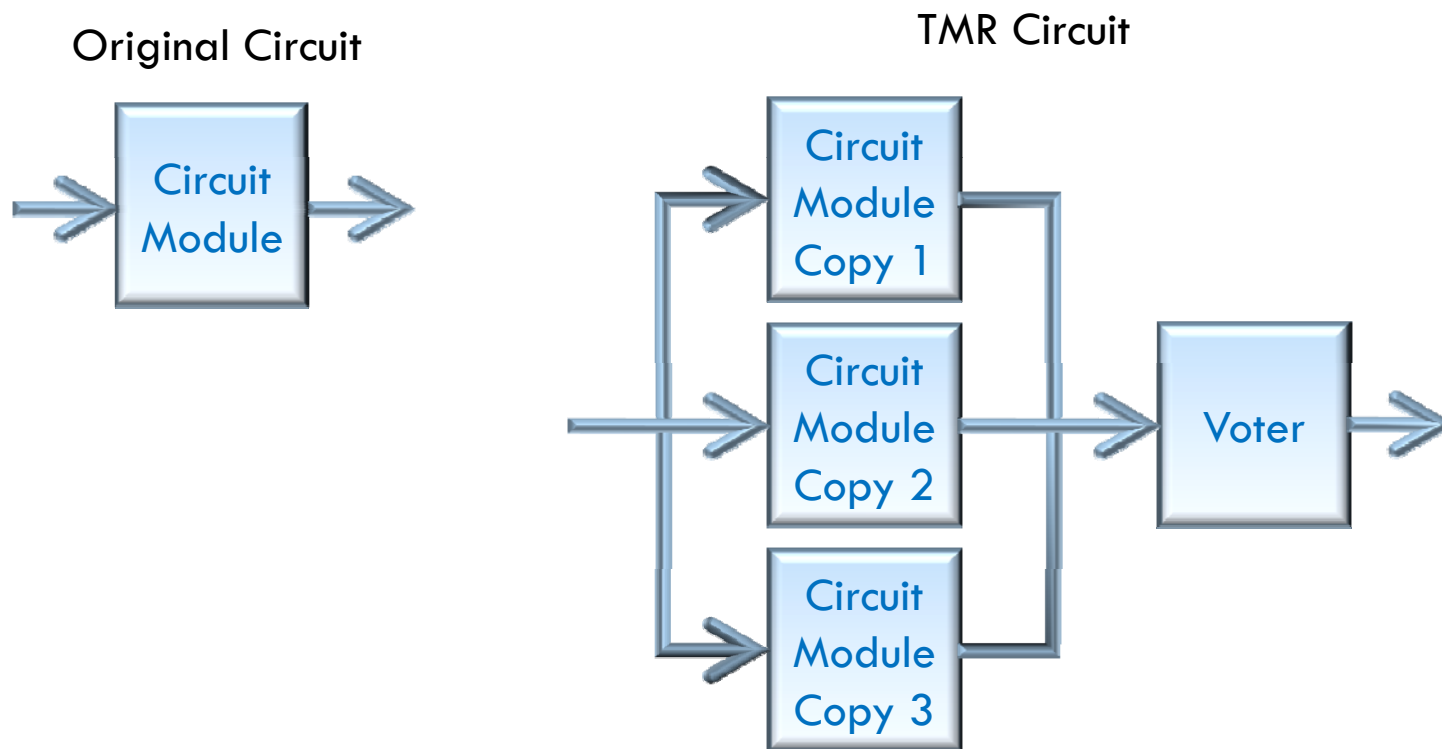
- A significant portion of SRAM-based FPGA memory cells are dedicated to user's circuit design (configuration memory)
- Upsets in the configuration memory can modify the actual operation of the circuit



Background :: Mitigating FPGA Radiation Effects

22

□ Triple Modular Redundancy



Note: In an FPGA, the XTMR style of TMR with triplicated voters must be employed to eliminate all single points of failure.



Background :: Mitigating FPGA Radiation Effects

23

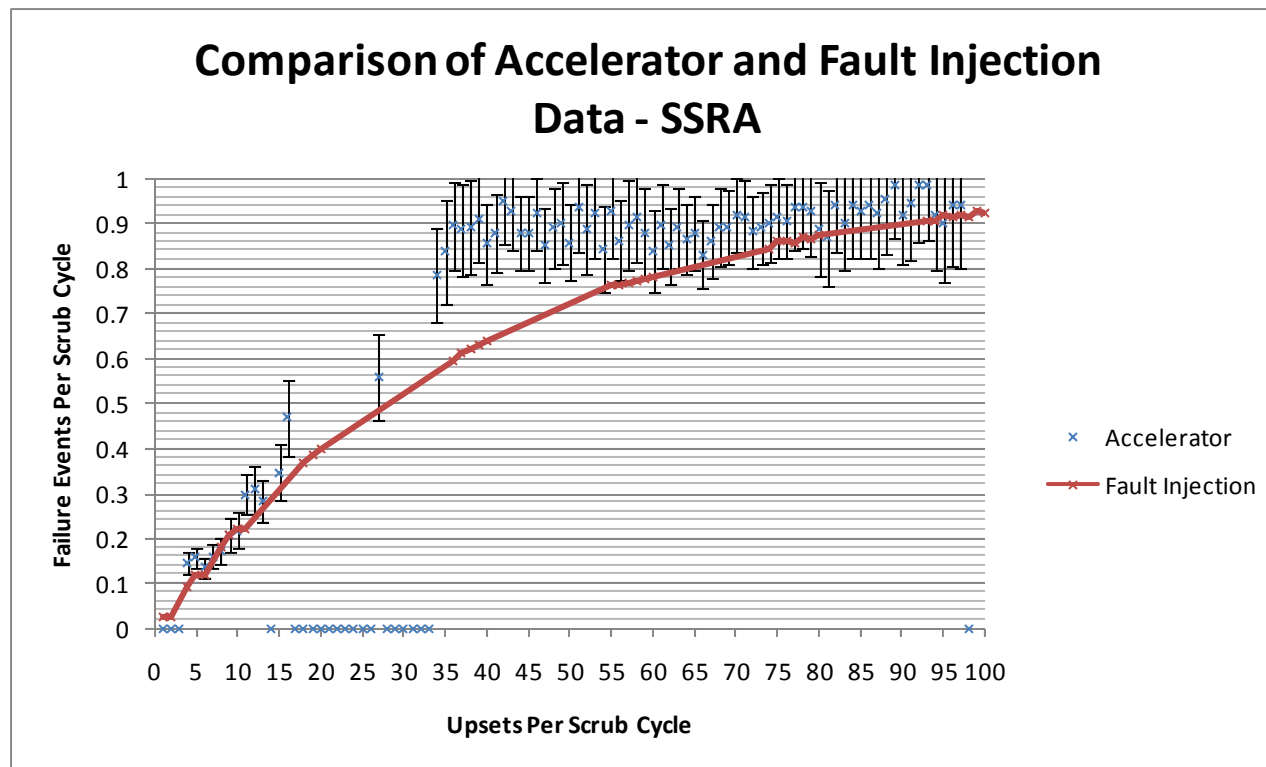
□ Scrubbing

- Periodic or continuous refresh of configuration memory back to intended state
- Prevents accumulation of upsets in configuration memory
- Reduces probability of simultaneous multiple independent upsets (MIUs) in configuration memory



Results :: Accelerator

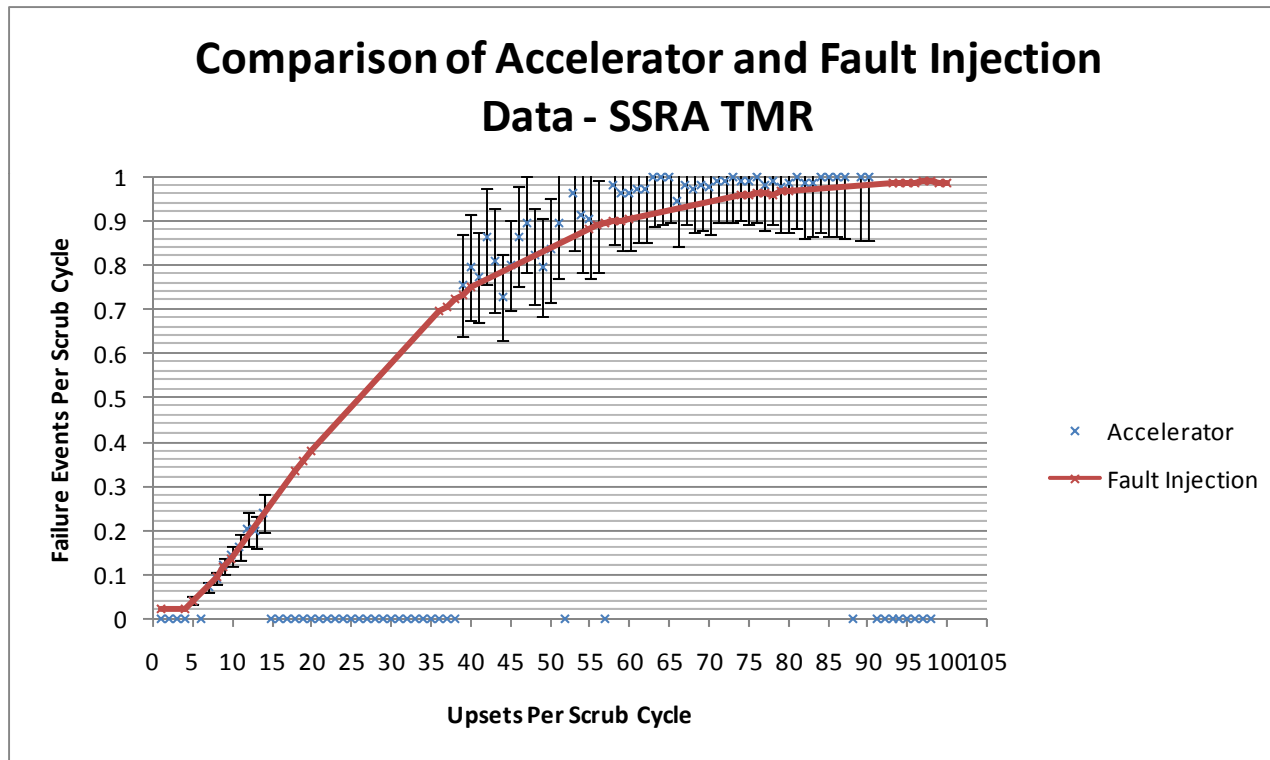
24



Note: minimum of 30 events were observed for each data point.



Results :: Accelerator



Note: minimum of 30 events were observed for each data point.



SEU Rate Models :: Logarithmic Fit SEU Rate Model

26

